| COS 226 Fall 2018 Class Exercise 17 | 5 questions; 4 pgs. |
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Today: Synthesis; review. §§ 19.*; 22.*.
Next class Synthesis; review. §§ 18.*; 21.*.
Reminders: Portfolio work; newsgroup; homework.

1. Write your group members' names below. Underline your name.
2. Depict all the stages in the restructuring of the following AA-tree when the key 1 is removed. It may be convenient to use dashed lines to separate tree levels, as in Andersson's paper. ${ }^{1}$


[^0]3. Depict the sequence of $A V L$ tree states resulting from the insertion of the following keys, in the order presented, into an initially empty tree.
$$
6,2,0,5,9,1,7,3,8,4
$$

You must depict intermediate tree states, including the state after each insertion, clearly marking and identifying each rotation.
4. Repeat Question 3 for bottom-up red-black trees. Follow the graphical conventions used in class: round nodes for red and boxed nodes for black. You must depict intermediate tree states, including the state after each insertion, clearly marking and identifying each rotation and color change.

## $6,2,0,5,9,1,7,3,8,4$

5. Repeat Question 3 for bottom-up splay trees,

You must depict intermediate tree states, including the state after each insertion, clearly marking and identifying each zig, zig-zig, and zig-zag operation.

$$
6,2,0,5,9,1,7,3,8,4
$$


[^0]:    ${ }^{1}$ Arne Andersson, "Balanced Search Trees Made Simple," in Proceedings of the Workshop on Algorithms and Data Structures (Montreal, Canada, 1993).

