## Name:

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1. (1 pt.)

- Read all material carefully.
- You may refer to your books, papers, and notes during this exam.
- No computer or network access of any kind is allowed (or needed).
- COS 480 students should answer non- $\star$ questions; $\star$ questions are for extra credit.
- COS 580 students should answer all questions, including $\star$ questions.
- Ambiguous or cryptic answers receive zero credit.
- Use the conventions used in class and the textbook.

Write your name in the space provided above.
2. ( 8 pts. ) Consider a directed graph with colored edges encoded by a relation Edge(S, D, color) with $(s, d, c) \in$ Edge iff there is a $c$-colored edge from vertex $s$ to vertex $d$. Write a Datalog query for the pairs of vertices $(x, y)$ such that there is a directed path from $x$ to $y$ but there is no alternating red-green path from $x$ to $y$. An alternating redgreen path is a path composed of only red- and green-colored edges with no consecutive edges of the same color. The vertices $x$ and $y$ in this definition need not be distinct. Explain your query briefly and prove that it is safe and stratified.
3. ( 5 pts.) Provide a SQL equivalent of the query of Question 2.
4. ( 8 pts.) Let $E$ denote an ER diagram composed of only entity sets (single and double boxes), relationships (single and double diamonds), and attributes on only entity sets. If $e, r$, and $a$ denote the number of entity sets, relationships, and attributes in $E$ then we may define the weight of $E$ to be $2 e+2 r+a$.
What is the minimum weight of such an ER diagram that includes at least one entity set whose key has at least 20 attributes? Justify your answer.
5. ( 8 pts.) Trace the naive evaluation of the query of Question 2 on the following instance.

| Edge |  |  |
| :---: | :---: | ---: |
| S | D | color |
| 1 | 2 | red |
| 1 | 5 | green |
| 2 | 3 | green |
| 2 | 4 | red |
| 3 | 1 | red |
| 3 | 2 | blue |
| 3 | 4 | green |
| 4 | 1 | red |
| 5 | 3 | red |

6. (10 pts.) $\star$ Repeat Question 5 for semi-naive evaluation.
