

4. Given a table `Edges(src, dst, color)` that encodes edges of a connected directed graph with colors as edge labels, write a recursive SQL query for pairs of vertices (a, b) such that there is a directed path composed of all red edges from a to b but no directed path from b to a .

5. State *Armstrong's Axioms* for functional dependencies and prove their soundness from first principles.